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| CZ4003 COMPUTER VISION - 2020 |
| Lab 2: Edge Detection + Hough Transform + 3D Stereo + Spatial Pyramid Matching  by  **B L**  **U-H**  Supervised by  **Prof Kemao &Prof Shijian**  Lenna - Wikipedia |
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# Edge Detection (Part 3.1a,b,c,d,e)

## Edge Detection: Sobel (Part 3.1a,b,c,d)

Sobel filter is an edge detector that works by determining the gradient (“the jump”) of image intensity. Sobel filter edge detector works because edges typically has the largest increase from light to dark.

Sobel filter works by using a vertical and horizontal edge detector:

|  |  |
| --- | --- |
| Vertical Gradient Filter (detect Horizontal edge) | Horizontal Gradient Filter (detect Verticle edge) |
|  |  |
| Results: Magnitude of Verticle Gradient | Results: Magnitude of Horizontal Gradient |
| Resultant Gradient Magnitude | |
|  | |
| Resultant Gradient Direction | |
|  | |

After convolution with the filter separately, we will have a map of the magnitudes of verticle gradient (from Vertical Edge Filter) and horizontal gradient (from Horizontal Edge Filter). The resultant gradient magnitude and orientation of the gradient can be determined as shown in the formula above. [1]

### Code (Part 3.1b,c)

|  |
| --- |
| % 3.1 b)  %Sobel Verticle and Horizontal Gradient Filter  s\_h=[-1 0 1;  -2 0 2;  -1 0 1;]  s\_v=[-1 -2 -1;  0 0 0;  1 2 1;]  %Verticle Filter  Pv=conv2(P,s\_v);  %Horizontal Filer  Ph=conv2(P,s\_h);    % 3.1 c)  %Magnitude of Gradient Map  P2=(Pv.^2.+Ph.^2).^0.5 |

### Results (Part 3.1b, Part 3.1c)

|  |  |
| --- | --- |
| Figure : Convolution with Vertical Filer (Part 3.1b) | Figure :Convolution with Horizontal Filer (Part 3.1b) |
| Figure : Map of the Magnitude of the Resultant Gradient | |

#### (Part 3.1b) What happens to edges which are not strictly vertical nor horizontal, i.e. diagonal?

After convolution with the **verticle gradient filter**, the image is a map of the magnitudes of verticle gradient (Figure 1).

Horizontal lines appear brighter while perfectly vertical lines are dark. The intensity of the **resultant verticle gradient map** changes from brightest when the line is horizontal to darkest when the line is verticle or if there is no change intensity of the original map. Edges that are diagonal appear less bright than a horizontal line.

After convolution with the **horizontal gradient filter**, the image is a map of the magnitudes of horizontal gradient (Figure 2).

Vertical lines appear brighter while perfectly horizontal lines are dark. The intensity of the **resultant verticle gradient map** changes from brightest when the line is Vertical to darkest when the line is horizontal or if there is no change intensity of the original map. Edges that are diagonal appear less bright than a Verticle line.

In the final resultant gradient magnitude map (Figure 3), all edges are detected both vertical and horizontal. Edges that are diagonal are also detected.

#### (Part 3.1c) Suggest a reason why a squaring operation is carried out.

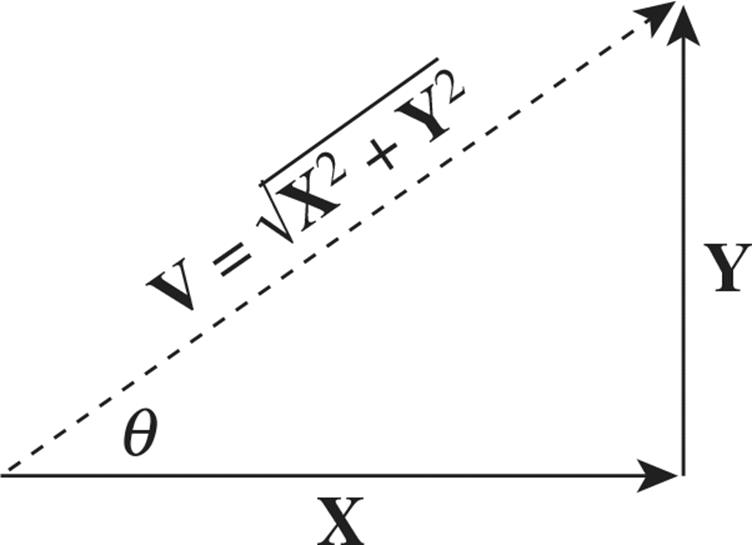


Figure : Resultant Vectors derived from horizontal and vertical components

The Squaring operation is carried and summed to obtain the resultant magnitude of the gradient. Because convolution with the **horizontal gradient filter** give the horizontal gradient vector. Convolution with the **verticle gradient filter** gives the verticle gradient vector. Therefore, we can use Pythagorean theorem to determine the resultant gradient (Figure 4).

#### (Part 3.1d) Vary Threshold: Try different threshold values and display the binary edge images.

##### Code

|  |  |
| --- | --- |
| % 3.1 d) Thresholding  min\_P2=double(min(P2(:)))%Min intensity=13  max\_P2=double(max(P2(:)))%Max intensity=204    %contrast stretching  P2C = (double(P2(:,:))-min\_P2).\*(255/(max\_P2-min\_P2));  %checking min max of P2  min(P2C(:)), max(P2C(:)) %0, 255 | Contrast stretch to make sure resultant gradient magnitude map is between 0 to 255 |
| t=OTSU\_B(P2C,true);  P2t=P2C>t;  [count,bins]=imhist(uint8(P2C),256); | Use OTSU to determine optimal threshold with minimal intra class variance/ maximum interclass variance  Refer to Appendix OTSU\_B.m. |
| figure( 'Position', [10 10 900 600]);  colormap('gray');imshow(P2t);title("Macritchie Sobel edge detector")  hold off;    t\_varry=linspace(10,220,8)  t\_varry=[t\_varry(1:2),t,t\_varry(3:7)]  figure( 'Position', [10 10 1440 960]);  for i = 1 : size(t\_varry,2)  P2t=P2C>t\_varry(i);  hold on  subplot(2,size(sigma\_varry,2)/2,i);colormap('gray');imshow(P2t);  if i==3  title({"Sobel" "t= " t\_varry(i),"OTSU"})  else  title(["Sobel" "t= " t\_varry(i)])  end  end  hold off | Plot out resulting sober filter after using different level of thresholding for binarization |

##### Results

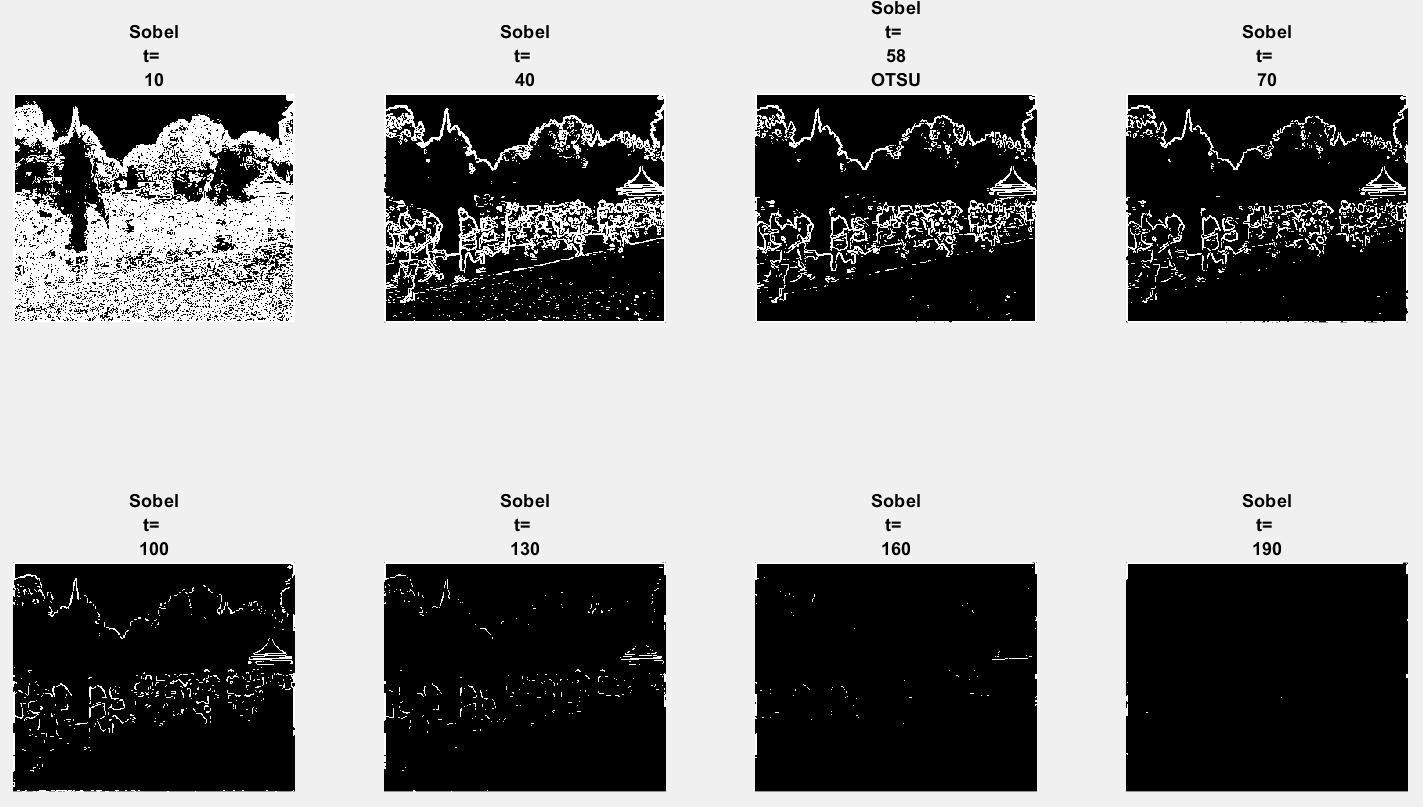


Figure : Sobel with different threshold

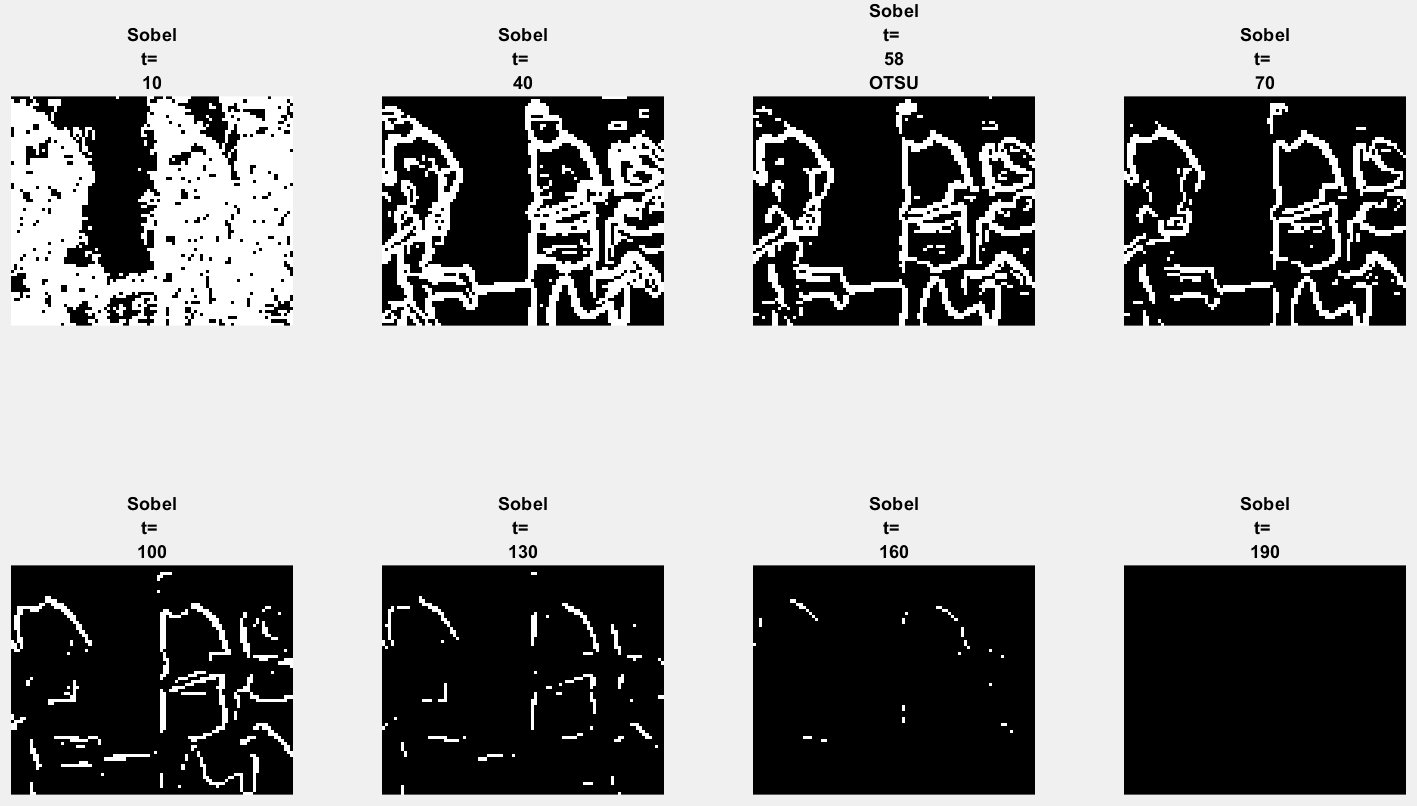


Figure : Sobel with different threshold zoom in

#### (Part 3.1 d )What are the advantages and disadvantages of using different thresholds?

Thresholding will help us to binarize the gradient map and help us identify likely edges. At lower threshold we obtain thicker lines (Figure 5, t=10)(Figure 6, t=10) while at higher thresholds we get thinner lines, and more lines is not detected(Figure 5, t=190)(Figure 6, t=190). To get the ‘optimal’ thresholding OTSU thresholding(Figure 5, t=58)(Figure 6, t=58). is implemented as a function

## Edge Detection: Canny edge detector (Part 3.1 e i ii )

### Code (Part 3.1e)

|  |
| --- |
| % 3.1 e)  tl=0.04, th=0.1, sigma=1.0;    E = edge(P,'canny',[tl th],sigma);  figure;colormap('gray');imshow(E);title("Macritchie Sobel edge detector") |

### Results (Part 3.1e)

|  |
| --- |
| Figure : Canny edge Detector ; |

### Vary : Code (Part 3.1ei)

|  |
| --- |
| % 3.1 e)i) Varry Sigma  sigma\_varry=linspace(1,5,5);  figure( 'Position', [10 10 1440 960]);  for i = 1 : size(sigma\_varry,2)  E = edge(P,'canny',[tl th],sigma\_varry(i));  hold on  subplot(2,3,i);colormap('gray');imshow(E);title(["Canny" "\sigma= " sigma\_varry(i)])  end  subplot(2,3,6);colormap('gray');imshow(P);title(["Original"])  hold off |

### Vary : Results (Part 3.1ei)

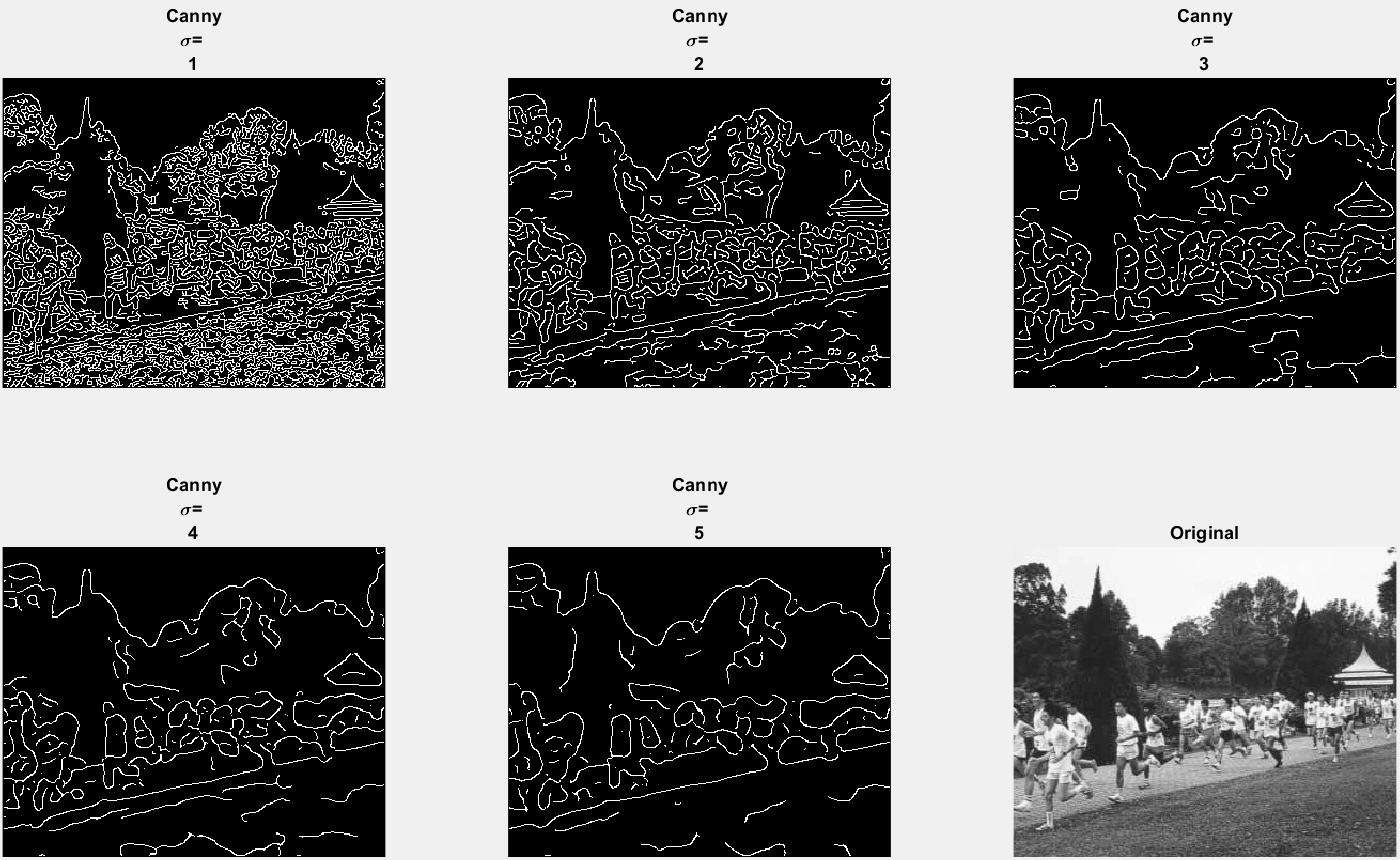


Figure : Canny Edge Detector varying

#### (Part 3.1 e i) What do you see and can you give an explanation for why this occurs? Discuss how different sigma are suitable for (a) noisy edgel removal, and (b) location accuracy of edgels.

As increases from 1 to 5 the sensitivity towards the edgel decreases. In other words, less edgel is detected. In terms of noise, less noisy edgel is detected. The location accuracy of the edgel also decreases. The reason for this is because gaussian edge filtering is able to remove noise. As, increases more **noise is removed(less noisy edgel is detected)** but it also means more details such as **edges is lost (location accuracy of the edgel also decreases)**.

If the original image is noisy and a lot of noisy edgel is detected, a larger sigma should be used to remove noisy edgel.   
If the original image is not noisy and we want to detect more edges with higher location accuracy, a of 1 should be sufficient.

### Vary : Code (Part 3.1eii)

|  |
| --- |
| % 3.1 e)i)Varry tl  tl\_varry=linspace(0.01,0.09,8);  figure( 'Position', [10 10 1440 960]);  for i = 1 : size(tl\_varry,2)  E = edge(P,'canny',[tl\_varry(i) th],sigma);  hold on  subplot(2,size(tl\_varry,2)/2,i);colormap('gray');imshow(E);title(["Canny" "th= " tl\_varry(i)])  end  hold off |

### Vary : Results (Part 3.1eii)

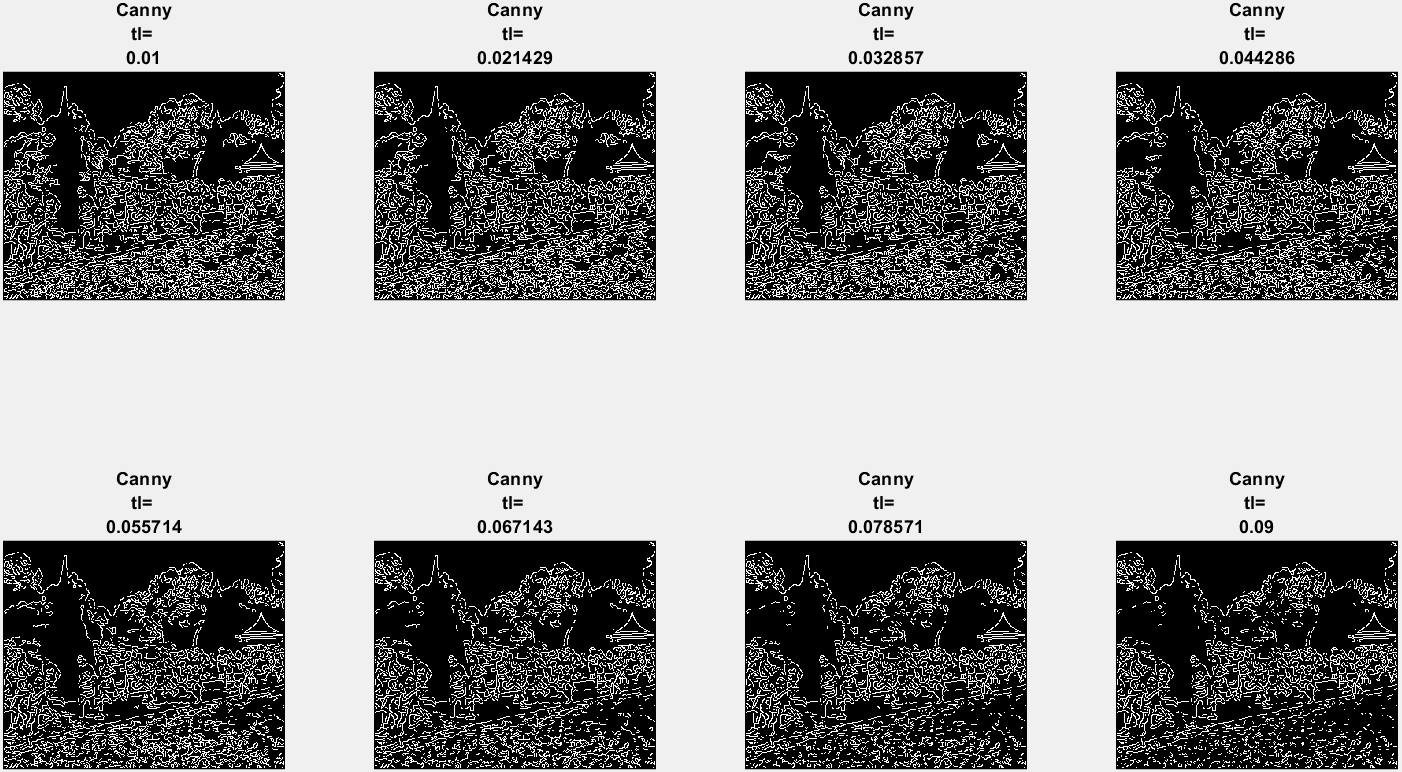


Figure : Canny Edge Detector varying tl

#### (Part 3.1 e ii ) Try raising and lowering the value of tl. What does this do? How does this relate to your knowledge of the Canny algorithm?

Raising the tl decreases the number of edges detected (Figure 9)

In Canny’s edge detector, hysteresis thresholding is employed.

* If a pixel is bellow tl, the pixel is set to 0.
* If a pixel is above tl and bellow th, the pixel is set to 1 if (Condition) its neighboring pixel perpendicular to the edge gradient have already been set to 1 .
* If a pixel is above th, the pixel is set to 0.

Therefore, increasing tl increases the threshold for edge detection and thus lesser edge is detected and lesser noisy edge is detected as well.

# Line Finding using Hough Transform (Part 3.2)

## (Part 3.2 b ) Read the help manual on Radon transform and explain why the transforms are equivalent in this case. When are they different? [2, 3, 4]

Radon Transform and Hough transform are mathematically similar

|  |  |
| --- | --- |
| **Radon Transform**  The Radon Projection is computed for a set of angle. “In general, the Radon transform of *f(x,y)* is the line integral of *f* parallel to the *y*´-axis. ” [2]    Figure : Geometry for Radon Transform  In other words, Radon Projection is like the **number of votes for a specific line represented in the parameter space in Hough Transform**.  “The Radon transform of an image is the sum of the Radon transforms of each individual pixel.” [2]  The magnitude of radon projection tell us the number of points that lie on the line perpendicular to  For instance, from Figure 10, “yellow amount” of points lie on the yellow dotted line which is a line perpendicular to x’.  It is important to note that | **Hough transform**  “*where  is the distance from the*[*origin*](https://en.wikipedia.org/wiki/Origin_(mathematics))*to the closest point on the straight line, and  (theta) is the angle between the axis and the line connecting the origin with that closest point*.” [5]    The fundamental idea is that any point can be described using a set of that describes a set of lines that intersects the point  “*Given a single point in the plane, then* ***the set of all straight lines going through that point corresponds to a***[***sinusoidal***](https://en.wikipedia.org/wiki/Sine_wave)***curve in the plane****, which is unique to that point. A set of two or more points that form a straight line will produce sinusoids which cross at that specific for that line. Thus, the problem of detecting*[*collinear points*](https://en.wikipedia.org/wiki/Line_(geometry)#Collinear_points)*can be converted to the problem of finding*[*concurrent*](https://en.wikipedia.org/wiki/Concurrent_lines)*curves*.” [5] |
| Algorithm  ***Step 1:*** The Radon transform is computed for a set of angle.  **For each angle,** the Radon transform of an image is the sum of the Radon transforms of each individual pixel.    The algorithm first divides pixels in the image into four subpixels and projects each subpixel separately, as shown in the following figure.    Figure : Radon projection magnitude map in a theta and x' array  ***Step 2:*** Radon projection magnitude can be map in a theta and x' array [2] | Algorithm  *The linear Hough transform*[*algorithm*](https://en.wikipedia.org/wiki/Algorithm)*uses a two-dimensional array, called an accumulator, to detect the existence of a line described by*  *The*[*dimension*](https://en.wikipedia.org/wiki/Dimension)*of the accumulator equals the two quantized values of and in the pair*  ***Step 1: For each pixel*** *at (x,y) the Hough Algorithm determines if there is enough evidence of a straight line at that pixel.*  ***Step 2:*** *If there is a line, it will calculate the parameters of lines that pass through that pixel and then increment the value of that corresponding bin in the accumulator*  ***Step 3:*** *Highest Values in the accumulator bin likely indicates a line can be extracted. The (approximate) geometric definition of that line in the x,y space can be derived from and*  *Due to* ***imperfection errors*** *in the edge detection step* ***(Step 2),***  *there will usually be errors in the accumulator space, which may make it not easy to find the appropriate peaks, and thus the appropriate lines.*  *“The final result of the linear Hough transform is a two-dimensional array (matrix) similar to the accumulator—one dimension of this matrix is the quantized angle and the other dimension is the quantized distance .*  *Each element of the matrix has a value equal to the sum of the points or pixels that are positioned on the line represented by quantized parameters So the element with the highest value indicates the straight line that is most represented in the input image.”* [5] |

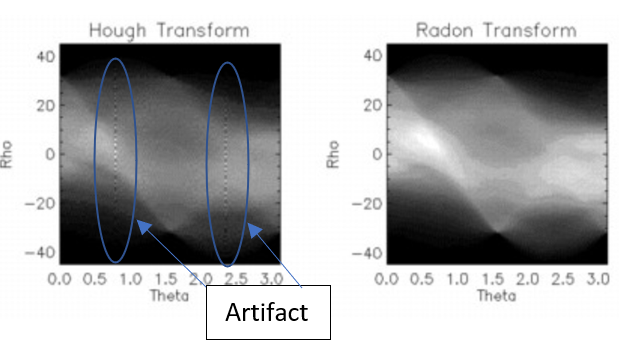
From this we see that magnitude in the parameter space is derived continuously (implemented discretely) using integration for Radon while, magnitude in the parameter space is derived discretely when using Hough Transform.

The difference in the Algorithm approach of mapping from the image space to a parameter space of ρ and θ is in their point of view.

* While the Radon transform derives the magnitude of a point in parameter space from image space (the *reading paradigm*) by using the radon projection transform on the image space,
* the Hough transform explicitly maps data points from image space to parameter space (the *writing paradigm*) when a line is detected. Magnitude of a point in a parameter space is derived by the accumulation of mapped points.

“Because of this, it is clear by comparing their (discrete) algorithms. For each θ in parameter space

* Radon projects the image points on a line described by (its angle) θ using buckets of size Δρ.
* Hough on the other hand takes each image point (x,y) and adds the appropriate intensity to all corresponding parameter space bins.



As a result Hough suffers artifacts whereas Radon allows for high resolution in parameter space (by adjusting Δθ and Δρ and dividing pixels into subpixels).” [4]

Therefore, in this case the transform is essentially equivilant because is discretized by a unit of 1. They will differ slightly if is discretized to smaller units.

(Note at the background, is discretized to smaller units but the radon Transform is presented with discretized to a unit of 1).

## Radon transform Code (Part 3.2 b and c)

|  |
| --- |
| %3.2 b  theta = 0:180;  [H, xp] = radon(E,theta);    figure( 'Position', [10 10 900 350]);  subplot(1,2,1);imagesc(theta,xp,H),colormap(gca), colorbar;  title('R\_{\theta} (X\prime)');  xlabel('\theta (degrees)')  ylabel('x''')  hold on;    %3.2 c  H\_max = max(H,[],'all')  [y,x]=find(H == H\_max)  hold off;    zoom=3  subplot(1,2,2);imagesc(theta(x-zoom:x+zoom),xp(y-zoom:y+zoom),H(y-zoom:y+zoom,x-zoom:x+zoom))  colormap(gca), colorbar  title({'Max R\_{\theta} (X\prime) =' num2str(H\_max),strcat("@ \theta= ", num2str(theta(x)), " and xp= ", num2str(xp(y)))});  xlabel('\theta (degrees)')  ylabel('x''')  hold on;  plot(theta(x),xp(y),'o',...  'MarkerEdgeColor','red',...  'MarkerFaceColor',[1 .6 .6]) |

## Radon transform Results (Part 3.2 b and c)

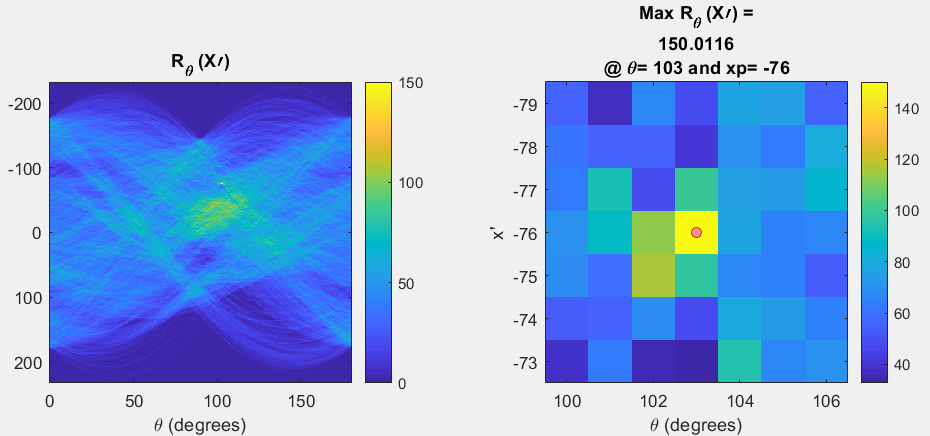


Figure : Results from Radon Transform (left) max intensity (right)

### (Part 3.2 c) Find the location of the maximum pixel intensity in the Hough image in the form of [theta, radius].

From the graph Figure 12, the maximum pixel intensity is 150.0116 at .

## (Part 3.2 d ) Derive the equations to convert the [theta, radius] line representation to the normal line equation form *Ax* + *By* = *C in image coordinates*.

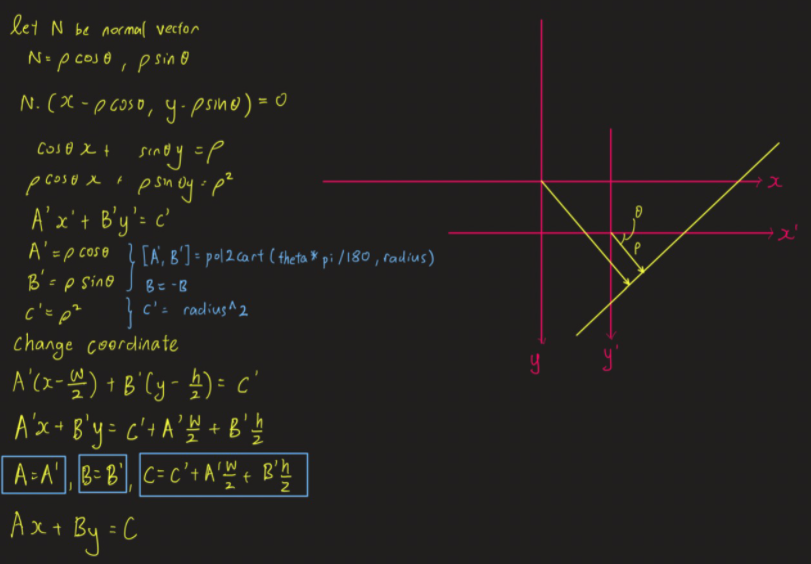


Figure : Derive the equations to convert the [theta, radius] line representation to the normal line equation form Ax + By = C in image coordinates.

### (Part 3.2 d) Show that A and B can be obtained via [6]

|  |  |
| --- | --- |
| >> [A, B] = pol2cart(theta\*pi/180, radius);  >> B = -B; |  |

Since pol2cart(theta, radius) converts polar coordinates to cartesian coordinate and it is shown in Figure 13 that A and B is the vector coordinates of P, therefore A and B can be obtained via the code above.

### Code: Line in Image plane (Part 3.2 d, e, f)

|  |
| --- |
| [A, B] = pol2cart(theta(x)\*pi/180, xp(y));  B=-B;  C=xp(y)^2+A\*size(P,2)/2+B\*size(P,1)/2;  y\_line=@(x) -A/B.\*x+C/B;  xl = 0,xr = size(P,2) - 1;  yl=y\_line(xl)  yr=y\_line(xr)  figure;colormap('gray');imshow(uint8(P));title("Macritchie (Finding Line)")  line([xl xr], [yl yr],'LineWidth',2); |

### Results: Line in Image plane (Part 3.2 d, e, f)

|  |  |
| --- | --- |
|  |  |

Figure : Line in Image Plane

#### (Part 3.2 f) Results: Does the line match up with the edge of the running path? What are, if any, sources of errors? Can you suggest ways of improving the estimation?

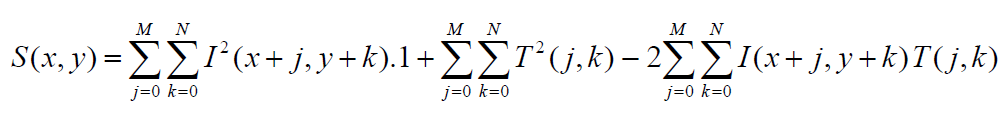
Yes. it matches up almost perfectly with the edge of the running path. But on closer inspection there is some deviation from the line on the right-hand side of the Image. This is likely because the running path is not a perfect straight line and therefore does will not match up with the perfect line.

The **possible sources of error** and suggested **improvements** are

1. The use of Radon to identify straight line introduced error in the detection of the straight line and this can be avoided by using a Generalized Hough Transform that can be used to detect curves
2. Another source of error may come from the discretization of the . This can be improved by using Radon transform with Xp discretized to smaller units rather than Hough transform.

# 3D Stereo (Part 3.2)

## Disparity Map Function (Part 3.2a)



|  |
| --- |
| function map = disparity\_map\_Barn(Pl, Pr, tempx,tempy)    [h, w] = size(Pl);  % Empty Map  map = ones(h, w);    %Half the size of template  half\_tx=floor(tempx/2);  half\_ty=floor(tempy/2);    max\_disparity=20;    for row = half\_tx+1:h-half\_tx  for xl = half\_ty+1:w-half\_ty  %Template  T = Pl(row-half\_ty:row+half\_ty,xl-half\_tx:xl+half\_tx);  %Since right point image will be more left than left point image  left = xl-max\_disparity;  right = xl;  if left<half\_tx+1  left = half\_tx+1;  end  ssd\_min = Inf;  xr\_min = left;  for xr = left:right  I = Pr(row-half\_ty:row+half\_ty,xr-half\_tx:xr+half\_tx);  ssd=sum(double(I).\*double(I),"All")-2\*sum(double(I).\*double(T),"All");  if ssd<ssd\_min  ssd\_min=ssd;  xr\_min = xr;  end  end  d = xl - xr\_min;  map(row, xl) = -d;  end  end  map=map(half\_tx+1:h-half\_tx, half\_ty+1:w-half\_ty);  end |

Function parameter

* Pl: gray scale left stereo image
* Pr: gray scale right stereo image
* tempx: width of template (left image)
* tempy: height of template (right image)

Avoided additional computation from fft and conv2 by using sum( , “All”) and element wise multiplication. Didn’t compute middle term because the middle term is a constant.

## Disparity Map Function on ‘corridorl.jpg’ and ‘corridorr.jpg’ (Part 3.2b, c, d)

### Code

|  |
| --- |
| %3.3 3D stereo  clear all;  %3.3 b  Pl = rgb2gray(imread('resource\corridorl.jpg'));  Pr = rgb2gray(imread('resource\corridorr.jpg'));  temp\_size=11;  half=floor(temp\_size/2);  whos Pl  whos Pr  figure;  subplot(1,2,1);colormap('gray');imshow(uint8(Pl));title("corridor left")  subplot(1,2,2);colormap('gray');imshow(uint8(Pr));title("corridor right")  %3.3 c  map=disparity\_map\_Barn(Pl,Pr,11,11);  figure;imshow(-map,[-15 15]);title({"Disparity Map","Max D=15"}) |

### Results (Part 3.2 c)

|  |  |
| --- | --- |
| Figure : Disparity Map | Figure : corridor\_disp.jpg |
| Figure : corridorl.jpg | |

### (Part 3.2 c) Comment on how the quality of the disparities computed varies with the corresponding local image structure.

Generally, as we move further away from the corridor, the disparity map becomes darker. This corresponds to reality because the distance is further away from the lens and thus disparity is smaller. The cone and sphere can be identified with the sphere being lighter and having a larger disparity than the cone. For the furthest most wall, because it seems the most homogeneous with even lighting, there seems to be some error in the where there is large disparity detected. The disparity map derived from SSD works best when there are more details or texture on the object.

## Rerun your algorithm on the real images of ‘triclops-i2l.jpg’ and triclops-i2r.jpg’.

### Results (Part 3.2 d)

|  |  |
| --- | --- |
| Figure : Disparity Map | Figure : triclopsid.jpg |
| Figure : triclopsi2l.jpg | |

### How does the image structure of the stereo images affect the accuracy of the estimated disparities?

Generally, the results show that objects closer to the lens have larger disparity and thus appear brighter while objects further away from the lens have smaller disparity and thus appear darker. There pavement does not seem to be properly mapped. One possible reason for this because we constrain the algorithm to only horizontal search. As you can see, there is **some rotation** between the left and the right image. Another possible reason for the poor disparity map of the pavement is due to the lack of very distinguishable features or edges that can help improve the robustness of the SSD this is in contranst to the vegetation on the left that seems to have a proper disparity map.

Also due to minimum disparity limit due to pixel size, the any object that is very far away will not be differentiated on the disparity map.

## Optional Bag of Words and Spatial Pyramid Matching

The section will reference the original article on SPM [7] and reference code from [8] to implement BOW and SPM.

### Summary

|  |  |  |  |
| --- | --- | --- | --- |
| Algorithm | BOW+ KNN | BOW+SVM | SPM (L=2) +SVM |
| Accuracy | 60% | 67% | 67-68% |

Refer to the sections bellow for proof of results

* *Results Bag of SIFT Representation + (KNN) Nearest Neighbor Classifier*
* *Results Bag of SIFT Representation + one-vs-all SVMs*
* *Spatial Pyramid Matching + one-vs-all SVMs*

### Algorithm

#### Bag of words

“Bag of words models are a popular technique for image classification inspired by models used in natural language processing. The model ignores or downplays word arrangement (spatial information in the image) and classifies based on a histogram of the frequency of visual words. The visual word "vocabulary" is established by clustering a large corpus of local features. See Szeliski chapter 14.4.1 for more details on category recognition with quantized features. In addition, 14.3.2 discusses vocabulary creation and 14.1 covers classification techniques.” [8]

Commonly in bag of words, huge data images is first vectorized using **SIFT. The vocabulary (features)** is extracted using K means clustering of the SIFT. Each K means represents a feature. Note the number of K means is selected by the programmer. In the code bellow we study how K means affect the accuracy of prediction. (Typically larger K, better accuracy because there is more features for prediction)

Using the set of K means/ features, feature histogram is formed for each image.

Using label training data set feature histogram and their corresponding label, a model can be trained either using KNN(K nearest neighbour) or SVM(Support vector Machine). Using the Trained Model, a prediction can be made on any input image. Note Typically (SVM models perform better than KNN)

#### Spatial Pyramid Matching

SPM builds on the same concepts of back of words by considering location of features. This is different from Bag of Words that sole depend on the histogram of features. In SPM, the same image is further sub divided into smaller images (Level 0=1 image, Level 1=4 image, Level 2=16 image, total 21 images). Each image is vectorized using SIFT and using K mean clustering, histogram features is formed for them. The histogram of features for the different level is then appended in a specific order.

### CODE

Note

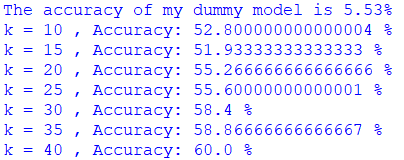
* Code was fully extracted from [8] with minor edits to reproduce accuracy of SPM for different levels L=0, L=1, L=2.
* Data was taken from [9] (source Caltect 101 [10])
* Explanations of flow of code for both BOW and SP and evaluations were added by me.

In the following code

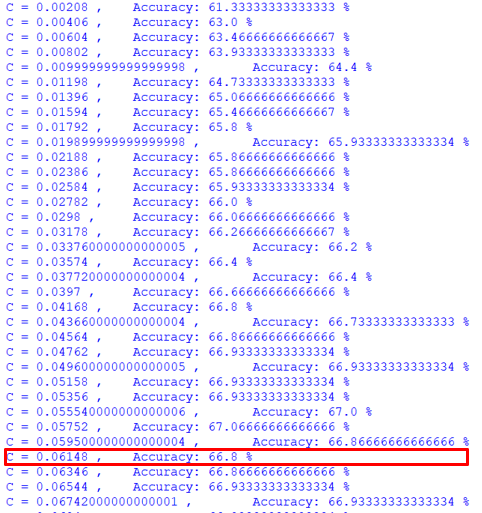
* BOW was implemented with KNN(K nearest neighbour) and SVM(Support vector Machine)
  + (Not related of KNN) Varying number of K-means clustering/ feature selected
  + Varying C in SVM to find optimal parameter for SVM
* Spatial Pyramid Matching was implemented with SVM(Support vector Machine)

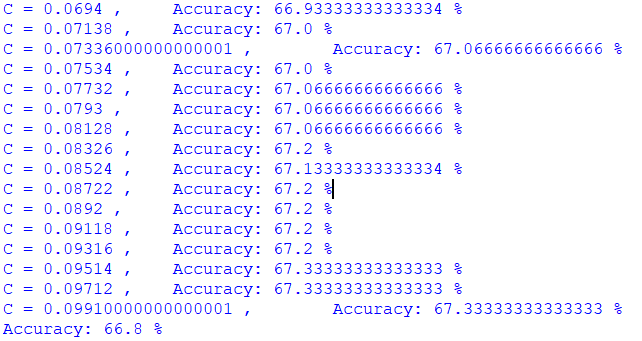
|  |  |
| --- | --- |
| Source: [8] | Explanations of flow of code for both BOW and SP and evaluations by me |
| 1. # import packages here 2. **import** cv2 3. **import** numpy as np 4. **import** matplotlib.pyplot as plt 5. **import** glob 6. #from scipy.misc import imresize  # resize images 7. **import** copy 8. **print**('OpenCv Version:',cv2.\_\_version\_\_) 10. class\_names = [name[11:] **for** name **in** glob.glob('data/train/\*')] 11. class\_names = dict(zip(range(0,len(class\_names)), class\_names)) 12. **print** (class\_names) |  |
| 1. ########################################################################### 2. **def** load\_dataset(path, num\_per\_class=-1): 3. data = [] 4. labels = [] 5. **for** id, class\_name **in** class\_names.items(): 6. img\_path\_class = glob.glob(path + class\_name + '/\*.jpg') 7. **if** num\_per\_class > 0: 8. img\_path\_class = img\_path\_class[:num\_per\_class] 9. labels.extend([id]\*len(img\_path\_class)) 10. **for** filename **in** img\_path\_class: 11. data.append(cv2.imread(filename, 0)) 12. **return** data, labels 14. # load training dataset 15. train\_data, train\_label = load\_dataset('data/train/', 100) 16. train\_num = len(train\_label) 17. **print** (train\_num) 18. # load testing dataset 19. test\_data, test\_label = load\_dataset('data/test/', 100) 20. test\_num = len(test\_label) | This section load data   1. train data, train label 2. test data, test label |
| 1. ########################################################################### 2. **from** sklearn.neighbors **import** KNeighborsClassifier 4. # train model 5. **def** trainKNN(data, labels, k): 6. neigh = KNeighborsClassifier(n\_neighbors=k, p=2) 7. neigh.fit(data, labels) 8. **return** neigh 9. ########################################################################### 10. #Bag of SIFT Representation + Nearest Neighbor Classifer 12. **from** sklearn.cluster **import** KMeans 13. **from** sklearn **import** preprocessing 15. # compute dense SIFT 16. **def** computeSIFT(data): 17. x = [] 18. **for** i **in** range(0, len(data)): 19. sift = cv2.xfeatures2d.SIFT\_create() 20. img = data[i] 21. step\_size = 15 22. kp = [cv2.KeyPoint(x, y, step\_size) **for** x **in** range(0, img.shape[0], step\_size) **for** y **in** range(0, img.shape[1], step\_size)] 23. dense\_feat = sift.compute(img, kp) 24. x.append(dense\_feat[1]) 26. **return** x 28. # extract dense sift features from training images 29. x\_train = computeSIFT(train\_data) 30. x\_test = computeSIFT(test\_data) 32. all\_train\_desc = [] 33. **for** i **in** range(len(x\_train)): 34. **for** j **in** range(x\_train[i].shape[0]): 35. all\_train\_desc.append(x\_train[i][j,:]) 37. all\_train\_desc = np.array(all\_train\_desc) 38. ########################################################################### 39. # build BoW presentation from SIFT of training images 40. **def** clusterFeatures(all\_train\_desc, k): 41. kmeans = KMeans(n\_clusters=k, random\_state=0).fit(all\_train\_desc) 42. **return** kmeans 43. ########################################################################### 44. # form training set histograms for each training image using BoW representation 45. **def** formTrainingSetHistogram(x\_train, kmeans, k): 46. train\_hist = [] 47. **for** i **in** range(len(x\_train)): 48. data = copy.deepcopy(x\_train[i]) 49. predict = kmeans.predict(data) 50. train\_hist.append(np.bincount(predict, minlength=k).reshape(1,-1).ravel()) 52. **return** np.array(train\_hist) 54. # build histograms for test set and predict 55. **def** predictKMeans(kmeans, scaler, x\_test, train\_hist, train\_label, k): 56. # form histograms for test set as test data 57. test\_hist = formTrainingSetHistogram(x\_test, kmeans, k) 59. # make testing histograms zero mean and unit variance 60. test\_hist = scaler.transform(test\_hist) 62. # Train model using KNN 63. knn = trainKNN(train\_hist, train\_label, k) 64. predict = knn.predict(test\_hist) 65. **return** np.array([predict], dtype=np.array([test\_label]).dtype)  68. **def** accuracy(predict\_label, test\_label): 69. **return** np.mean(np.array(predict\_label.tolist()[0]) == np.array(test\_label)) 70. ########################################################################### 72. k = [10, 15, 20, 25, 30, 35, 40] 73. **for** i **in** range(len(k)): 74. kmeans = clusterFeatures(all\_train\_desc, k[i]) 75. train\_hist = formTrainingSetHistogram(x\_train, kmeans, k[i]) 77. # preprocess training histograms 78. scaler = preprocessing.StandardScaler().fit(train\_hist) 79. train\_hist = scaler.transform(train\_hist) 81. predict = predictKMeans(kmeans, scaler, x\_test, train\_hist, train\_label, k[i]) 82. res = accuracy(predict, test\_label) 83. **print**("k =", k[i], ", Accuracy:", res\*100, "%") | Bag of SIFT Representation + Nearest Neighbor Classifier  1. **Vectorise Image** by converting image to dense SIFT    * computeSIFT(data)      + return SHIFT data x 2. **build BoW** presentation from SIFT of training images    * clusterFeatures(all\_train\_desc, k)      + return k means      + K means clustering to for k number of means (k features) from SIFT 3. **form training set histograms** for each training image using BoW representation    * def formTrainingSetHistogram(x\_train, kmeans, k):      + return histogram of features      + using SIFT predict closest k mean and fill up feature histogram 4. **build histograms for test set** and **predict using KNN**    * def predictKMeans(kmeans, scaler, x\_test, train\_hist, train\_label, k):      + return test set prediction      + Use KNN(K nearest neighbours) different from K mean clustering.        - k-NN is a supervised algorithm used for classification        - For each evaluation matrix, Decide upon the value of k. Here k refers to the number of closest neighbors we will consider while doing the majority voting of target labels.        - Run k-NN a few times, changing k and checking the evaluation measure.        - In each iteration, k neighbors vote, majority vote wins and becomes the ultimate prediction        - Optimize k by picking the one with the best evaluation measure.        - Once you’ve chosen k, use the same training set and now create a new test set with the people’s ages and incomes that you have no labels for, and want to predict.      + Train KNN using train\_hist and train\_label      + Use trained KNN to predict test\_hist's label 5. **evaluate accuracy** of predict test\_hist's label    * def accuracy(predict\_label, test\_label):      + return correct label/ total test label |
| 1. #Bag of SIFT Representation + one-vs-all SVMs 3. **from** sklearn.svm **import** LinearSVC 5. k = 60 6. kmeans = clusterFeatures(all\_train\_desc, k) 8. # form training and testing histograms 9. train\_hist = formTrainingSetHistogram(x\_train, kmeans, k) 10. test\_hist = formTrainingSetHistogram(x\_test, kmeans, k) 12. ########################################################################### 13. # normalize histograms 14. scaler = preprocessing.StandardScaler().fit(train\_hist) 15. train\_hist = scaler.transform(train\_hist) 16. test\_hist = scaler.transform(test\_hist) 17. ########################################################################### 18. #Train one-vs-all SVMs using sklearn 20. **for** c **in** np.arange(0.0001, 0.1, 0.00198): 21. clf = LinearSVC(random\_state=0, C=c) 22. clf.fit(train\_hist, train\_label) 23. predict = clf.predict(test\_hist) 24. **print** ("C =", c, ",\t Accuracy:", np.mean(predict == test\_label)\*100, "%") 25. ########################################################################### 26. #We can train 15 SVM classifiers manually and get same result 28. y\_train\_global = np.zeros((len(train\_label), 1)) 29. y = copy.deepcopy(y\_train\_global) 31. y\_predict = np.zeros((len(test\_label), 1)) 32. **for** i **in** range(len(test\_label)): 33. index = 0 34. test = np.array([test\_hist[i,:]]).T 35. **for** j **in** range(len(class\_names)): 36. y = copy.deepcopy(y\_train\_global) 37. y[index:index+100, 0:1] = np.ones((100,1)) 38. clf = LinearSVC(random\_state=0, C=0.06148) 39. clf.fit(train\_hist, y.ravel()) 40. **if** j == 0: 41. maxScore = np.dot(clf.coef\_, test) + clf.intercept\_ 42. y\_predict[i, 0:1] = j 43. **elif** np.dot(clf.coef\_, test) + clf.intercept\_ > maxScore: 44. maxScore = np.dot(clf.coef\_, test) + clf.intercept\_ 45. y\_predict[i, 0:1] = j 46. index = index + 100 47. **print** ("Accuracy:", np.mean(y\_predict.ravel() == test\_label)\*100, "%") | Bag of SIFT Representation + one-vs-all SVMs  1. (Same)**Vectorise Image** by converting image to dense SIFT    * computeSIFT(data)      + return SHIFT data x 2. (Same)**build BoW** presentation from SIFT of training images    * clusterFeatures(all\_train\_desc, k)      + return k means      + K means clustering to for k number of means (k features) from SIFT 3. (Same)**form training and test set histograms** for each training image using BoW representation    * def formTrainingSetHistogram(x\_train, kmeans, k):      + return histogram of features      + using SIFT predict closest k mean and fill up feature histogram 4. **Use 1 v All SVM (Support Vector Machine) to train and predict**    * clf = LinearSVC(random\_state=0, C=c)    * clf.fit(train\_hist, train\_label)    * predict = clf.predict(test\_hist)      + Large Value of parameter C => small margin      + Small Value of paramerter C => Large margin        - find optimal smallest c (largest margin) value for training data set so that misclassification of test data set is lower. In order words, it gerneralised the SVM model for other data sets other than training data set source: Medium 5. (Same)**evaluate accuracy** of predict test\_hist's label    * def accuracy(predict\_label, test\_label):      + return correct label/ total test label |
| 1. ########################################################################### 2. **import** itertools 3. **from** sklearn.metrics **import** confusion\_matrix 5. **def** plot\_confusion\_matrix(cm, classes, 6. normalize=False, 7. title='Confusion matrix', 8. cmap=plt.cm.Blues): 9. """ 10. This function prints and plots the confusion matrix. 11. Normalization can be applied by setting `normalize=True`. 12. """ 13. **if** normalize: 14. cm = cm.astype('float') / cm.sum(axis=1)[:, np.newaxis] 15. #print("Normalized confusion matrix") 17. #print(cm) 19. plt.imshow(cm, interpolation='nearest', cmap=cmap) 20. plt.title(title) 21. plt.colorbar() 22. tick\_marks = np.arange(len(classes)) 23. plt.xticks(tick\_marks, classes, rotation=45) 24. plt.yticks(tick\_marks, classes) 26. fmt = '.2f' **if** normalize **else** 'd' 27. thresh = cm.max() / 2. 28. **for** i, j **in** itertools.product(range(cm.shape[0]), range(cm.shape[1])): 29. plt.text(j, i, format(cm[i, j], fmt), 30. horizontalalignment="center", 31. color="white" **if** cm[i, j] > thresh **else** "black") 33. plt.tight\_layout() 34. plt.ylabel('True label') 35. plt.xlabel('Predicted label') 37. # Compute confusion matrix 38. cnf\_matrix = confusion\_matrix(np.array([test\_label]).T, y\_predict) 39. np.set\_printoptions(precision=2) 41. # Plot non-normalized confusion matrix 42. plt.figure(figsize=(18, 6)) 43. plot\_confusion\_matrix(cnf\_matrix, classes=class\_names, 44. title='Confusion matrix, without normalization') 46. # Plot normalized confusion matrix 47. plt.figure(figsize=(18, 6)) 48. plot\_confusion\_matrix(cnf\_matrix, classes=class\_names, normalize=True, 49. title='Normalized confusion matrix') 51. plt.show() | Plot Confusion Matrix for Bag of SIFT Representation + one-vs-all SVMs **REFER TO RESULTS :** *“Results Bag of SIFT Representation + one-vs-all SVMs”* |
| 1. #Improve performance with Spatial Pyramid Matching 3. **import** math 5. **def** extract\_denseSIFT(img): 6. DSIFT\_STEP\_SIZE = 2 7. sift = cv2.xfeatures2d.SIFT\_create() 8. disft\_step\_size = DSIFT\_STEP\_SIZE 9. keypoints = [cv2.KeyPoint(x, y, disft\_step\_size) 10. **for** y **in** range(0, img.shape[0], disft\_step\_size) 11. **for** x **in** range(0, img.shape[1], disft\_step\_size)] 13. descriptors = sift.compute(img, keypoints)[1] 15. #keypoints, descriptors = sift.detectAndCompute(gray, None) 16. **return** descriptors  19. # form histogram with Spatial Pyramid Matching upto level L with codebook kmeans and k codewords 20. **def** getImageFeaturesSPM(L, img, kmeans, k): 21. W = img.shape[1] 22. H = img.shape[0] 23. h = [] 24. **for** l **in** range(L+1): 25. w\_step = math.floor(W/(2\*\*l)) 26. h\_step = math.floor(H/(2\*\*l)) 27. x, y = 0, 0 28. **for** i **in** range(1,2\*\*l + 1): 29. x = 0 30. **for** j **in** range(1, 2\*\*l + 1): 31. desc = extract\_denseSIFT(img[y:y+h\_step, x:x+w\_step]) 32. #print("type:",desc is None, "x:",x,"y:",y, "desc\_size:",desc is None) 33. predict = kmeans.predict(desc) 34. histo = np.bincount(predict, minlength=k).reshape(1,-1).ravel() 35. weight = 2\*\*(l-L) 36. h.append(weight\*histo) 37. x = x + w\_step 38. y = y + h\_step 40. hist = np.array(h).ravel() 41. # normalize hist 42. dev = np.std(hist) 43. hist -= np.mean(hist) 44. hist /= dev 45. **return** hist  48. # get histogram representation for training/testing data 49. **def** getHistogramSPM(L, data, kmeans, k): 50. x = [] 51. **for** i **in** range(len(data)): 52. hist = getImageFeaturesSPM(L, data[i], kmeans, k) 53. x.append(hist) 54. **return** np.array(x) 56. ########################################################################### 57. k = 200 58. kmeans = clusterFeatures(all\_train\_desc, k) 59. ########################################################################### 60. train\_histo = getHistogramSPM(2, train\_data, kmeans, k) 61. test\_histo = getHistogramSPM(2, test\_data, kmeans, k) 62. ########################################################################### 63. # train SVM 64. **for** c **in** np.arange(0.000307, 0.001, 0.0000462): 65. clf = LinearSVC(random\_state=0, C=c) 66. clf.fit(train\_histo, train\_label) 67. predict = clf.predict(test\_histo) 68. **print** ("C =", c, ",\t\t Accuracy:", np.mean(predict == test\_label)\*100, "%") | Improve performance with Spatial Pyramid Matching  1. (Same done)**Vectorise Image** by converting image to dense SIFT    * computeSIFT(data)      + return SHIFT data x 2. (Same 200 features SHIFT data)**build BoW** presentation from SIFT of training images    * clusterFeatures(all\_train\_desc, k)      + return k means      + K means clustering to for k number of means (k features) from SIFT 3. (different)**form training and test set feature histograms** for each training image using BoW representation    * **getHistogramSPM(L, data, kmeans, k)**      + return SPM Histogram        - return combined SPM Histogram        - ↑ **getImageFeaturesSPM(L, img, kmeans, k)**          * return SPM Histogram for each all level of spaces in the spacial pyramid.          * For L=0: 1 image, L=1: 4image, L=2: 16image          * ↑ **extract\_denseSIFT(img)** 4. (same) **Use 1 v All SVM (Support Vector** Machine) to train and predict    * clf = LinearSVC(random\_state=0, C=c)    * clf.fit(train\_hist, train\_label)    * predict = clf.predict(test\_hist)      + Large Value of parameter C => small margin      + Small Value of paramerter C => Large margin        - find optimal smallest c (largest margin) value for training data set so that misclassification of test data set is lower. In order words, it gerneralised the SVM model for other data sets other than training data set source: Medium 5. (Same)evaluate accuracy of predict test\_hist's label    * def accuracy(predict\_label, test\_label):      + return correct label/ total test label |

### Results Bag of SIFT Representation + (KNN) Nearest Neighbor Classifier



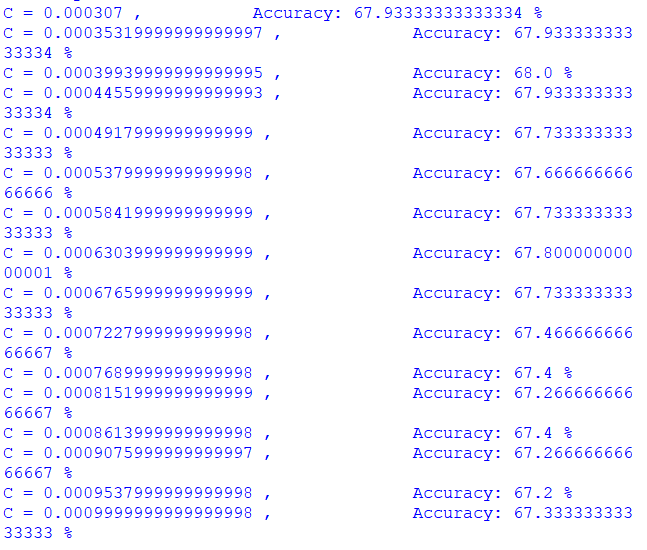
### Results Bag of SIFT Representation + one-vs-all SVMs





|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
|  | |  |  |  |  | | --- | --- | --- | --- | | 0 | Bedroom | 8 | Mountain | | 1 | Coast | 9 | Office | | 2 | Forest | 10 | OpenCountry | | 3 | Highway | 11 | Store | | 4 | Industrial | 12 | Street | | 5 | InsideCity | 13 | Suburb | | 6 | Kitchen | 14 | TallBuilding | | 7 | LivingRoom |  |  | |
|  |  |

#### Results for Spatial Pyramid Matching + one-vs-all SVMs



# Appendix

## OTSU\_B.m

|  |  |
| --- | --- |
| function threshold =OTSU\_B(gray, Analysis)  %OTSU Thresholding  %Maximise interclass variance  size(count)  inter\_class\_var=zeros(size(bins,1),1);  for n=1:size(bins,1)  %Mean of L(backgnd)and H(foregnd)  mean\_L=dot(count(1:n),bins(1:n))/sum(count(1:n));  mean\_H=dot(count(n+1:256),bins(n+1:256))/sum(count(n+1:256));  weight\_L=sum(count(1:n))/sum(count);  weight\_H=sum(count(n+1:256))/sum(count);  inter\_class\_var(n)=weight\_L\*weight\_H\*(mean\_L-mean\_H)^2;  end  [M,I] = max(inter\_class\_var)  %Analysis Report | Maximize intraclass variance |
| if Analysis ==true  %Plot Interclass variance  figure( 'Position', [10 10 900 600]);    subplot(1,2,1);plot(bins,inter\_class\_var);  hold on;  plot(bins(I),inter\_class\_var(I),'o',...  'MarkerEdgeColor','red',...  'MarkerFaceColor',[1 .6 .6])  title({'Inter class variance','{\sigma}^2-{\sigma \_w}^2={W}\_L{W}\_H({\mu \_L}+{\mu \_H})^2'})  xlabel('Threshold, t');  ylabel('Inter class variance, {\sigma}^2-{\sigma \_w}^2');    %Plot histogram with OTSU threshold    subplot(1,2,2);imhist(uint8(gray),256);title("Histogram with OTSU Threshold");  hold on;  xline(bins(I),'-r',{'OTSU Threshold',strcat('t= ',num2str(bins(I)))})  end    threshold=bins(I)  end | Analysis produce   * interclass variance vs threshold plot and * image histogram with threshold |

# References

|  |  |
| --- | --- |
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